The System **SOL** version 2025

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SOL is a Haskell-based tool for showing confluence and strong normalisation of higher-order computation. SOL is intended to be a generic higher-order computation analysis tool that is applicable to the modern theories of higher-order programming languages. This aim is demonstrated in [Ham19] and further developed in [HAK20].

Based on the foundation of second-order algebraic theories [FH10] and its computational counter part [Ham19] and polymorphic extension [HAK20], we have implemented various results on higher-order syntax and computation in SOL, including Knuth and Bendix's critical pair checking for confluence.

Recently, Muroya and Hamana have proposed a framework referred to as Term Evaluation Systems (TERS), unifying operational semantics and refinement reasoning [MH24]. We have also implemented contextual improvement verification by critical pair analysis [MH24] in SOL. Since every context-sensitive rewriting system can be simulated by a nondeterministic term evaluation system, in the present SOL 2025 version, we have implemented confluence checking of context-sensitive rewriting on an experimental basis.

References

- [MH24] Koko Muroya and M. Hamana. Term Evaluation Systems with Refinements: First-Order, Second-Order, and Contextual Improvement, *Proc. of 17th International Symposium on Functional and Logic Programming (FLOPS 2024)*, Lecture Notes in Computer Science 14659, pp. 31-61, Springer, 2024.
- [FH10] M. Fiore and C.-K. Hur. Second-order equational logic. In Proc. of CSL'10, LNCS 6247, pages 320–335, 2010.
- [Ham19] M. Hamana. How to prove decidability of equational theories with second-order computation analyser SOL. Journal of Functional Programming, Cambridge University Press, Vol. 29, e20, 2019.
- [HAK20] Makoto Hamana, Tatsuya Abe, and Kentaro Kikuchi.
 Polymorphic Computation Systems: Theory and Practice of Confluence with Call-by-value,
 Science of Computer Programming, Elsevier, Volume 187, 102322, 15 February 2020.