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# infChecker at CoCo 2022

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## Description

- infChecker is a tool for checking **(in)feasibility of goals**  
 $\mathcal{G} = \{F_i\}_{i=1}^m$ , where  $F_i = (s_{ij} \bowtie_{ij} t_{ij})_{i=1}^{n_i}$ .
- $\bowtie_{ij}$  represents **predicates** on terms defined by provability of goals  $s \bowtie_{ij} t$  with respect to a *first-order theories*  $\text{Th}_{\bowtie_{ij}}$ .
- $\bowtie_{ij}$  can be one of the following predicates:
  - One (CS-)rewriting step ( $\rightarrow$ ,  $\rightarrow$ ).
  - Zero or more (CS-)rewriting steps ( $\rightarrow^*$ ,  $\rightarrow^*$ ).
  - One or more (CS-)rewriting steps ( $\rightarrow^+$ ,  $\rightarrow^+$ ).
  - Subterm ( $\mid \geq$ ) and strict subterm ( $\mid >$ ).
  - (CS-)Joinability ( $\rightarrow^* \leftarrow$ ,  $\rightarrow^* \leftarrow$ ).
  - One (CS-)convertibility step ( $\leftarrow \rightarrow$ ,  $\leftarrow / \rightarrow$ ).
  - Zero or more (CS-)convertibility steps ( $\leftarrow \rightarrow^*$ ,  $\leftarrow / \rightarrow^*$ ).

# Implementation

- The tool is available here:  
`http://zenon.dsic.upv.es/infChecker/`.
- It is written in Haskell and provides a first implementation of the **Feasibility Framework**, where four **processors** have been implemented:
  - $P^{\text{Sat}}$  integrates a satisfiability approach to **prove infeasibility using model generators** as AGES and Mace4 to find a proof.
  - $P^{\text{UR}}$  **simplifies** problems by removing non-usable rules.
  - $P^{\text{Prov}}$  integrates a logic-based approach to program analysis to **prove feasibility by theorem proving**. In infChecker, we use the theorem prover Prover9.
  - $P^{\text{NC}}$  adapt the processor that **narrow conditions** in the 2D DP framework for proving operational termination of CTRs to be used with feasibility sequences.

# Strategy and Results

- Our **proof strategy** is:
  - 1 we apply  $P^{UR}$  whenever it is sound and complete;
  - 2 we try to prove feasibility using  $P^{Prov}$ ;
  - 3 if  $P^{Prov}$  fails, we apply  $P^{Sat}$ ;
  - 4 if  $P^{Sat}$  fails, we apply  $P^{NC}$ ;
  - 5 if  $P^{NC}$  succeeds and modifies the feasibility sequence, we repeat the strategy, otherwise we return `MAYBE`.
- Bibliography:
  - GL20** R. Gutiérrez and S. Lucas. Automatically Proving and Disproving Feasibility Conditions. In Proc. of IJCAR'2020, LNCS 12167:416–435. Springer, 2020.
  - Luc19** S. Lucas. Proving semantic properties as first-order satisfiability. Artificial Intelligence 277, paper 103174, 24 pages, 2019.
  - LG18** S. Lucas and R. Gutiérrez. Use of Logical Models for Proving Infeasibility in Term Rewriting. Information Processing Letters, 136:90-95, 2018.